

# Interfaces for High-Speed Fiber-Optic Links: Analysis and Experiment

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**Abstract**—An analysis of directly and externally modulated fiberoptic links is presented here. The theoretical analysis is based on the signal flow diagram of the interface circuits to the laser diode, Mach-Zehnder electro-optic modulator, and p-i-n photodiode. System parameters such as gain, noise figure, two-tone intermodulation distortion, and spurious free and compression dynamic range are expressed as a function of frequency and operating point of the laser and external modulator. Two directly and externally modulated fiber-optic links were designed and fabricated to verify the analytical models. The direct modulation FO link was developed at the *Ku*-band (11.6–12.4 GHz), whereas the external modulation link was at *L*-band (875–925 MHz). Spurious-free dynamic ranges of  $95.8 \text{ dB} \cdot \text{Hz}^{2/3}$  and  $113 \text{ dB} \cdot \text{Hz}^{2/3}$ , respectively, were achieved, the best reported to date for these frequency bands. The predictions based on the analytical models match the measured results very well.

## INTRODUCTION

HIGH-SPEED fiber-optic links are envisioned as playing a major role in many microwave circuits and systems [1]. Some potential applications include antenna remoting and distribution networks [2], delay lines [3], and optical control of microwave devices [4]. Accurate modeling of the FO link performance will aid the system designer in evaluating the suitability of the viable architectures to specific applications. Most of the fiber-optic links designed for microwave applications are relatively short to medium length (up to 1 km) and employ intensity detection techniques. The intensity modulation of light is realized via either direct modulation of a semiconductor laser diode or external modulation of laser light by taking advantage of the interaction of light with matter. Of the various external modulation schemes, the most common presently use travelling-wave or lumped-element Mach-Zehnder modulators that operate using the electro-optic properties of  $\text{LiNbO}_3$  [5] or GaAs [6].

Until now, there has not been a full analytical model for direct and external modulation fiber-optic links that

presents the important link parameters—such as gain, noise figure, two-tone intermodulation distortion, compression and spurious free dynamic range—in a language accessible to the microwave engineer. Even though attempts to explain the link performance in terms of equivalent circuit parameters have been made [7]–[11], these models suffer from inaccurate prediction of broadband FO link performance. Some even have incorrect physical circuit models with unreasonable component values. Thus, the goal of this paper is to present the analytical models necessary to predict FO link performance. Furthermore, analytical models are used as guidelines to develop low loss, high dynamic range FO links. The experimental results are compared to the analytical models' predictions to verify the models.

## DEVICE CHARACTERIZATION AND MODELING

An essential part of low-loss, high dynamic range FO link design is the development of reactively matched interface circuits, which are only realizable when the transducer characteristics at microwave frequencies are known. Design steps involve the characterization and modeling of the semiconductor laser diode and electro-optic modulator as the microwave/optical transducer portions of the two types of optical transmitters. By contrast, an impedance-matched p-i-n photodiode constitutes the optical/microwave transducer in the optical receiver for both architectures. Standard TRL de-embedding techniques are adequate for extracting the intrinsic transducer's impedance at microwave frequencies from the measured impedance of the device in its test fixture. The de-embedded impedance is then fitted to an equivalent circuit model over a broad bandwidth by the use of a realistic physical model.

The conceptual block diagram of the direct modulation optical transmitter at microwave frequencies, Fig. 1, shows an impedance matching circuit with the laser equivalent circuit model and the corresponding signal flow diagram. The circuit elements are based on the physical parameters of the laser and their values are obtained from the TRL de-embedding of the intrinsic laser impedance. The goal of the matching network is to effectively transfer current at the design frequency band from the  $50 \Omega$

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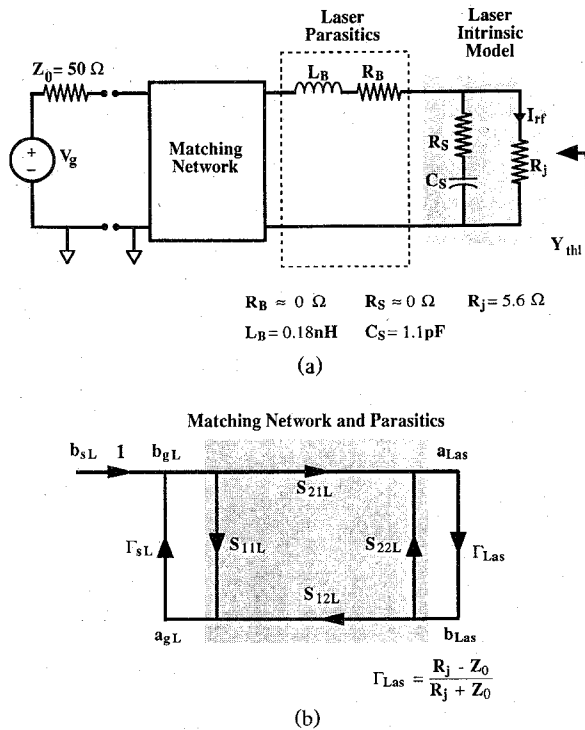


Fig. 1. Semiconductor laser diode as the microwave/optical interface. (a) Intrinsic and extrinsic equivalent circuit model with values for a Ku-band link. (b) Signal flow diagram model.

system input to the junction of the laser diode, denoted by the current  $I_{rf}$  passing through the forward-biased p-n junction resistance  $R_j$ . Since  $R_j$  is less than  $10\ \Omega$ , the matching network is effectively a  $50\ \Omega$  to approximately  $10\ \Omega$  impedance transformer. The minimum reflection coefficient attainable using reactive matching techniques will be limited by the quality factor of the laser and the percentage bandwidth over which impedance-matching is performed; for example, the theoretical limit for minimum return loss achieved over a 2–4 GHz bandwidth for a buried hetero-junction semiconductor laser (such as Ortel's SL1000H) is  $-14\ \text{dB}$ .

The optical transmitter module of an externally modulated FO link, Fig. 2, shows the equivalent circuit of a lumped-element Mach-Zehnder modulator and the signal flow diagram of the transmitter. The impedance matching network in the Mach-Zehnder modulator transforms the input signal so that at the design frequency band maximum voltage  $V_m$  is obtained across the capacitor  $C_m$ . The lumped series resistance  $R_m$ , with typical values of about 5 to 6  $\Omega$ , forms the effective load resistance. The limitation imposed on the impedance matching network is by the quality factor of the external modulator determined by  $C_m$  and  $R_m$ . For example, the lumped-element  $\text{LiNbO}_3$  Mach-Zehnder modulator used in the 875–925 MHz link has a minimum return loss of  $-11.6\ \text{dB}$  across the band. Using reactive matching networks results in satisfactory matching.

A block diagram of the optical receiver module, Fig. 3, shows a p-i-n photodiode equivalent circuit model and the

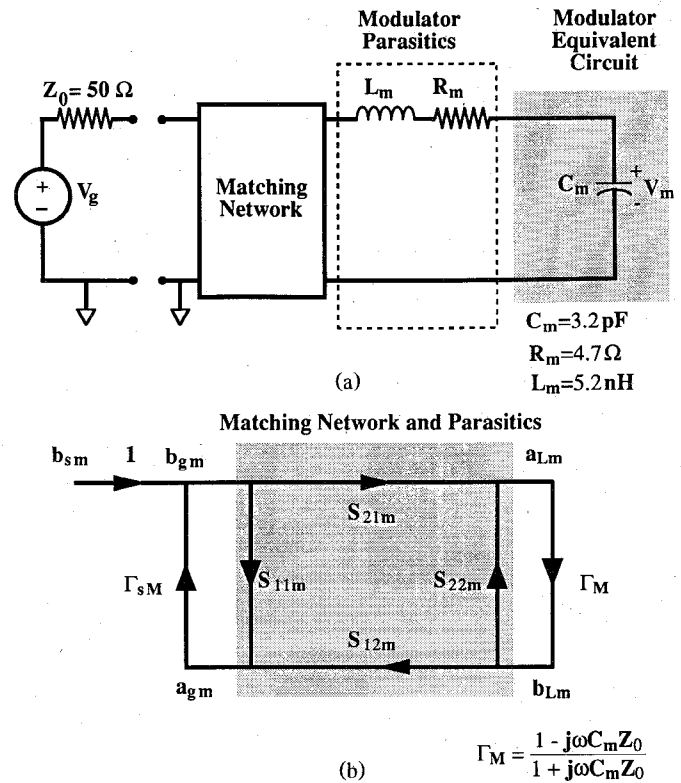


Fig. 2. Mach-Zehnder lumped-element external electro-optic modulator as the microwave/optical interface. (a) Intrinsic and extrinsic equivalent circuit model with values for an L-band link. (b) Signal flow diagram model.

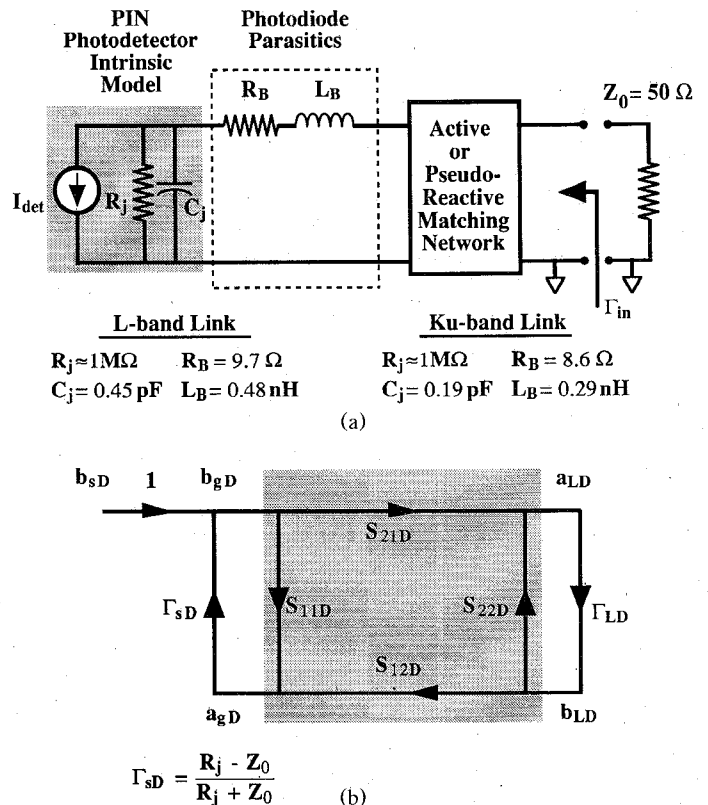


Fig. 3. p-i-n photodiode as the optical/microwave interface. (a) Intrinsic and extrinsic equivalent circuit model. (b) Signal flow diagram model.

receiver matching network. The goal of the matching circuit is to effectively transform the RF photocurrent  $I_{\text{det}}$  to the 50  $\Omega$  load. Ideally, an impedance matching network for the receiver would entail the matching of the photodiode's high shunt junction resistance  $R_j$ —typically 1 M $\Omega$ —to the output of the FO link, which is a 50  $\Omega$  system. The quality factor of the photodiode is extremely high if parasitics are small. However, the de-embedding and equivalent circuit modeling of the photodetectors reveals that the parasitic series resistance dominates over the reverse-biased p-n junction resistance at microwave frequencies. This series resistance,  $R_B$ , therefore dictates a lower overall  $Q$ -factor. Thus it is the series resistance  $R_B$  that is transformed to 50  $\Omega$  in the detector's impedance matching network. For example, in the case of the InGaAs p-i-n photodiode used in the 11.6–12.4 GHz link, de-embedding and equivalent circuit modeling yielded  $R_j$  of approximately 1 M $\Omega$ ,  $C_D = 0.19$  pF, and a parasitic series resistance  $R_B = 8.6$   $\Omega$ . Across the 11–13 GHz band, therefore, the best achievable return loss is –20.2 dB. However, over broad bandwidths active matching techniques using MESFET's leads to improved return loss for the optical receiver.

#### DIRECTLY MODULATED FO LINKS

##### Gain Analysis

The gain of a fiber-optic link can be calculated in terms of microwave scattering parameters using the signal flow diagram (SFD) technique. The transducer gains of the optical transmitter and optical receiver are derived separately and then combined to yield the gain of the complete link. When a directly modulated semiconductor laser diode is employed in the optical transmitter, the SFD is obtained by considering the forward-bias junction resistance of the laser diode to be the port two termination  $\Gamma_{\text{Las}}$  of a two-port network (represented by  $[S_L]$ ) consisting of the microwave impedance-matching circuit and other device parameters of the laser. Fig. 1 shows the schematic diagram and SFD for the transmitter in a direct modulation link. The output power of a fiber-optic link depends on the amplitude of photocurrent,  $I_{\text{det}}$ , generated in the detector, which is in turn proportional to the RF current,  $I_{\text{rf}}$ , through the laser diode's active region. This RF current is expressed as

$$I_{\text{rf}} = \sqrt{Y_0} (a_{\text{Las}} - b_{\text{Las}}), \quad (1)$$

where  $a_{\text{Las}}$  and  $b_{\text{Las}}$  are of the normalized input and output powers, respectively, at the laser junction resistance, and  $Y_0$  is the characteristic admittance of the transmitter input (i.e., 20 mS for a standard 50  $\Omega$  system). From the SFD it is clear that

$$\begin{aligned} a_{\text{Las}} &= \frac{I_{\text{rf}}^+}{\sqrt{Y_0}} = \frac{b_{\text{SL}} S_{21L}}{(1 - S_{22L} \Gamma_{\text{Las}})} \quad \text{and} \\ b_{\text{Las}} &= \frac{I_{\text{rf}}}{\sqrt{Y_0}} = \frac{b_{\text{SL}} S_{21L} \Gamma_{\text{Las}}}{(1 - S_{22L} \Gamma_{\text{Las}})}. \end{aligned} \quad (2)$$

By definition, the power delivered to the laser junction is the difference between the incident and reflected powers, i.e.:

$$P_{\text{out},Tx} = |a_{\text{Las}}|^2 - |b_{\text{Las}}|^2 = \frac{|b_{\text{SL}}|^2 \times |S_{21L}|^2 \times |1 - \Gamma_{\text{Las}}|^2}{|1 - S_{22L} \Gamma_{\text{Las}}|^2}. \quad (3)$$

Hence the transducer gain of the directly modulated laser-based optical transmitter is

$$G_{Tx} = \frac{P_{\text{out},Tx}}{|b_{\text{SL}}|^2} = \frac{|S_{21L}|^2 \times |1 - \Gamma_{\text{Las}}|^2}{|1 - S_{22L} \Gamma_{\text{Las}}|^2}. \quad (4)$$

The link current transfer function,  $H_L$ , is defined as the ratio of detector current  $I_{\text{det}}$  to RF current  $I_{\text{rf}}$  across the laser and is given by

$$\begin{aligned} \left( \frac{P_{\text{in},RX}}{P_{\text{out},TX}} \right) &= \frac{|I_{\text{det}}|^2}{|I_{\text{rf}}|^2} = |H_L|^2 \\ &= (\eta_L K_L L K_D \eta_D)^2 |H_{\text{Las}}(f, I_b)|^2 |H_{\text{det}}(f, V_b)|^2, \end{aligned} \quad (5)$$

where  $\eta_L$  is the laser diode external quantum efficiency,  $\eta_D$  is the photodetector responsivity,  $L$  is the optical attenuation in the fiber, and  $K_L, K_D$  are the laser-to-fiber and fiber-to-detector coupling efficiencies, respectively.  $|H_{\text{Las}}(f, I_b)|^2$  and  $|H_{\text{det}}(f, V_D)|^2$  are the frequency transfer characteristics of the laser and photodetector, respectively, for the given operating biases. For links operating well below the observable 3-dB bandwidth in the laser and detector frequency responses, these two terms are both approximately unity.

When a reverse-biased p-i-n photodiode is employed in the optical receiver, the SFD is obtained by considering the junction resistance of the diode to be the source termination  $\Gamma_{\text{SD}}$  of a two-port network (represented by  $[S_D]$ ) consisting of the other device parameters of the photodetector and the microwave impedance-matching circuit. Fig. 3 shows the schematic diagram and SFD for the optical receiver. The output microwave power is derived from the SFD and from the square root of the incident and reflected detector powers ( $a_{LD}$  and  $b_{LD}$ , respectively) as follows:

$$P_{\text{out}} = |a_{LD}|^2 - |b_{LD}|^2 = |a_{LD}|^2 = \frac{|b_{\text{SD}}|^2 \times |S_{21D}|^2}{|1 - S_{11D} \Gamma_{\text{SD}}|^2}, \quad (6)$$

since  $b_{LD} = 0$ . Therefore,

$$G_{Rx} = \frac{P_{\text{out}}}{|b_{\text{SD}}|^2} = \frac{|S_{21D}|^2}{|1 - S_{11D} \Gamma_{\text{SD}}|^2}. \quad (7)$$

The transducer gain of the direct modulation link is thus obtained from the optical transmitter and receiver gains

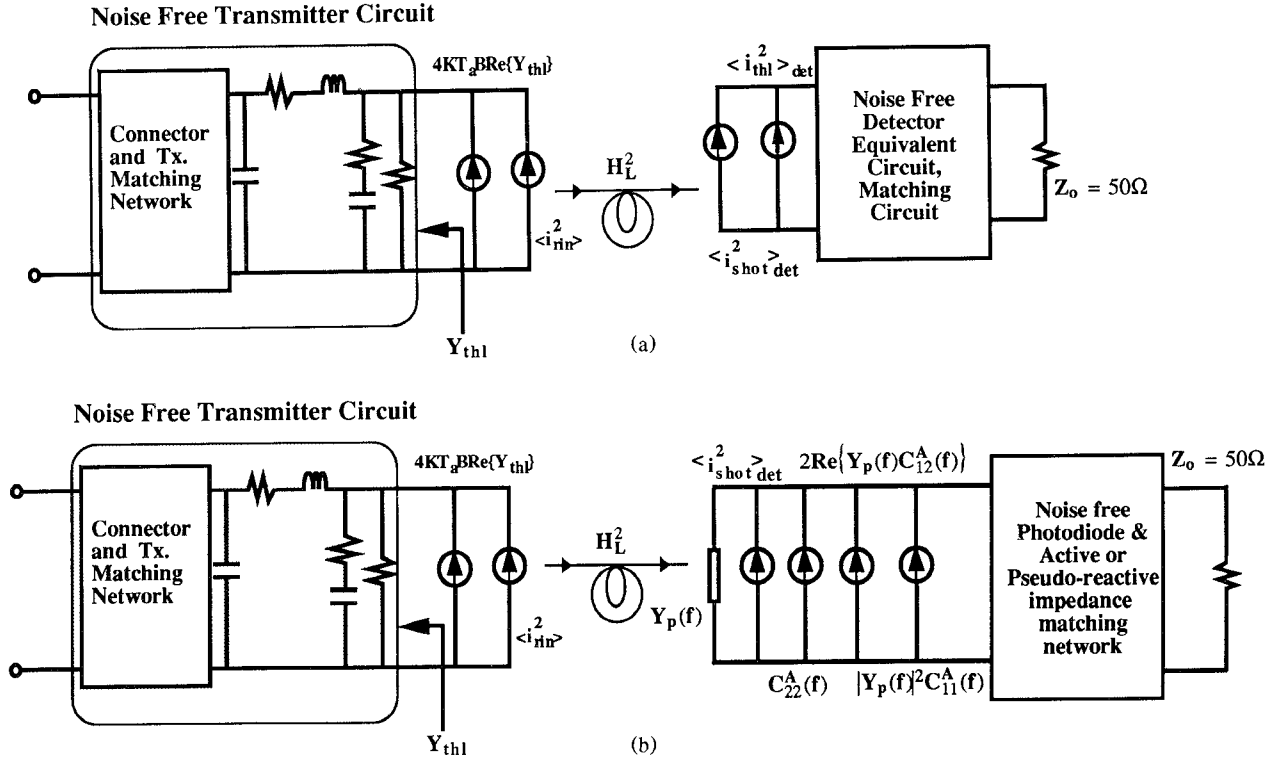


Fig. 4. Schematic representation of noise sources in a directly modulated FO link. (a) With a reactively matched receiver. (b) With an actively matched receiver.

and the square of the link current transfer function; i.e., the thermal noise is obtained as

$$G = \frac{P_{out, Rx}}{P_{av, Tx}} = G_{Tx} \cdot H_L^2 \cdot G_{Rx}$$

$$= \frac{|S_{21L}|^2 |S_{21D}|^2 |1 - \Gamma_{Las}|^2 (\eta_L K_L L K_D \eta_D)^2}{|1 - \Gamma_{Las} S_{22L}|^2 |1 - \Gamma_{sD} S_{11D}|^2} \quad (8)$$

#### Noise Analysis

Three categories of noise sources, shown in Fig. 4, contribute to the total noise powers in the directly modulated FO link, viz. thermal, shot, and relative intensity noise of laser. The various noise sources of the link are derived as follows:

The thermal noise powers of the transmitter and receiver are calculated using the Nyquist theorem [12] by assuming that each of the individual noise sources in any circuit can be represented by an equivalent noise power at the input or output of the circuit, provided the individual noise sources are uncorrelated. By representing the noise power in this fashion the rest of the circuit can be considered to be noise-free. As shown in Fig. 4, an equivalent thermal noise current source is obtained from the total conductance,  $\text{Re}\{Y_{th}\}$ , of the transmitter circuit as seen from the transmitter output. Using the transfer function of the link from the transmitter output to the output of the receiver, the power output of the transmit-

$$N_{thtx} = 4kT_a B (\eta_L K_L L K_D \eta_D)^2 \text{Re}\{Y_{th}\} \frac{|S_{21D}|^2}{|1 - \Gamma_{sD} S_{11D}|^2} Z_o, \quad (9)$$

where  $B$  is the resolution bandwidth of the receiver,  $k$  is Boltzmann's constant,  $T_a$  is the ambient temperature, and  $Z_o$  is the impedance of the output termination ( $50\Omega$ ).

A major noise source in direct modulation FO links is the semiconductor laser's relative intensity noise (RIN), which arises from the statistical fluctuations of the photon and electron generation rates within the laser. The RIN, which is a function of frequency and bias current, can be calculated from the laser's physical parameters [13]. This RIN is then represented as a current source at the transmitter output whose amplitude is dependent on both frequency ( $f$ ) and laser dc bias current ( $I_b$ ). Noise power at the output of the direct modulation link due to laser RIN is calculated as

$$N_{RIN} = \text{RIN}(f, I_b) (I_b - I_{th})^2 (\eta_L K_L L K_D \eta_D)^2 \cdot \frac{|S_{21D}|^2}{|1 - \Gamma_{sD} S_{11D}|^2} B Z_o, \quad (10)$$

where  $I_{th}$  is the laser threshold current.

The shot noise of the photodiode, like the laser's RIN, makes a major contribution to the total noise output of the link. The total shot noise power in terms of the dc

current detected by the photodiode and the photodiode's dark current ( $I_d$ ) is given as

$$N_{\text{shot}} = 2e[(I_b - I_{\text{th}})(\eta_L K_L L K_D \eta_D) + I_d] \cdot B \frac{|S_{21D}|^2}{|1 - \Gamma_{sD} S_{11D}|^2} Z_0, \quad (11)$$

where  $e$  is the electronic charge.

The thermal noise of the reactively matched detector makes a negligible contribution to the total link noise output power; it can be calculated as

$$N_{\text{thrx}} = 2kT_a B(1 - |\Gamma_{\text{in}}|^2), \quad (12)$$

where  $\Gamma_{\text{in}}$  is the reflection coefficient looking into the impedance-matched photodetector circuit from its output.

The total noise power at the output of the detector is the sum of all these individual noise powers,

$$N_{\text{out}} = N_{\text{RIN}} + N_{\text{shot}} + N_{\text{thtx}} + N_{\text{thrx}} = N_{\text{RIN}} + N_{\text{shot}} + N_{\text{th}}. \quad (13)$$

The noise analysis with active matching circuit (shown in Fig. 4b) in the receiver circuit is complicated, due to the fact that the noise sources of the active elements are correlated and cannot be added individually. The correlation matrix in the A-representation, for a MESFET, is as follows [14]:

$$C_{11}^A = 2kT_a \cdot R_n \quad (14)$$

$$C_{22}^A = 2kT_a \cdot R_n \cdot |Y_{\text{opt}}|^2 \quad (15)$$

$$C_{21}^A = 2kT_a [0.5(F_{\text{min}} - 1) - R_n \cdot Y_{\text{opt}}] \quad (16)$$

$$C_{12}^A = C_{21}^{A*} \quad (17)$$

where  $F_{\text{min}}$  is the minimum noise figure of the MESFET;  $R_n$  is the equivalent noise resistance; and  $Y_{\text{opt}}$  is the optimum source admittance.  $C_{11}^A$  and  $C_{22}^A$  are the autocorrelations of the noise voltage and noise current source, respectively, and  $C_{21}^A$  is the correlation between the voltage and current source. For the MESFET, we can define an equivalent noise current at the input of the receiver in terms of an autocorrelation spectrum of the equivalent noise current as

$$C^I(f) = C_{22}^A(f) + 2\text{Re}\{Y_p(f)C_{12}^A(f)\} + |Y_p(f)|^2 C_{11}^A(f), \quad (18)$$

where  $Y_p(f)$  is the input admittance of the MESFET. The noise power due to the FET at the output of the detector is given by

$$N_{\text{FET}} = C^I(f) \cdot B \cdot \frac{|S_{21D}|^2}{|1 - \Gamma_{sD} S_{11D}|^2} Z_0. \quad (19)$$

The thermal noise of the transmitter circuitry  $N_{\text{thtx}}$ , the laser's RIN noise power  $N_{\text{RIN}}$  and the shot noise of the photodiode  $N_{\text{shot}}$  are as given by (9)–(11). The link ther-

mal noise due to the detector and its matching circuitry, not considering that of the MESFET, is negligible and is not considered here. Thus the total noise output of the link is given as

$$N_{\text{out}} = N_{\text{thtx}} + N_{\text{RIN}} + N_{\text{shot}} + N_{\text{FET}}. \quad (20)$$

Since the thermal noise source at the input of the link is expressed as  $N_{\text{in}} = kT_a B$ , the noise figure of the fiber-optic link now can be defined as

$$NF_{\text{Link}} \equiv \frac{(SNR)_{\text{in}}}{(SNR)_{\text{out}}} = \frac{P_{\text{in}} \cdot N_{\text{out}}}{P_{\text{out}} \cdot N_{\text{in}}} = \frac{1}{G_{\text{Link}}} \cdot \frac{N_{\text{out}}}{N_{\text{in}}}. \quad (21)$$

### Distortion Analysis

The distortion characteristics in a direct modulation link are analyzed with respect to the current modulation index  $m$  of the laser which is given as  $m = I_{\text{rf}} / (I_b - I_{\text{th}})$ . The term IMD/C is defined as the power ratio between the optical third order intermodulation product and the fundamental of the optical signal. The total optical power out of the laser for a two tone input signal is given as [15], [16]:

$$P(t) = \frac{P_0}{I_0(a_1)I_0(a_2)} \left[ I_0(a_1)I_0(a_2) + 2I_0(a_2) \sum_{k=1}^{\infty} I_k(a_1) \cos k(\omega_1 t + \theta_1) + 2I_0(a_1) \sum_{n=1}^{\infty} I_n(a_2) \cos n(\omega_2 t + \theta_2) + 4 \sum_{k=1}^{\infty} I_k(a_1) \cos k(\omega_1 t + \theta_1) \cdot \sum_{n=1}^{\infty} I_n(a_2) \cos n(\omega_2 t + \theta_2) \right] \quad (22)$$

where  $I_x(a_i)$  are modified Bessel functions of the  $x$ th order and  $a_i$ , for  $i=1,2$ , can be obtained from the following equation:

$$m_i = a_i \sqrt{\left( \frac{\omega_i^2}{\omega_0^2} - \phi(a_i) \right)^2 + \omega_i^2 \tau_p^2 \left( \frac{1}{\omega_0^2 \tau_p \tau_s} + 1 \right)^2} \quad (23)$$

where, for  $i=1,2$ :  $m_i$  is the optical modulation index;  $\omega_i = 2\pi f_i$ ;  $f_i$  is the input signal frequency;  $\omega_0 = 2\pi f_0$ ;  $f_0$  is the relaxation oscillation frequency;  $\tau_p$  is the photon lifetime in the cavity;  $\tau_s$  is the spontaneous emission lifetime;  $\tau_p$  and  $\tau_s$  are calculated from the laser's physical parameters [16]. The term  $\phi(a_i)$  is defined as

$$\phi(a_i) = \frac{2I_1(a_i)}{a_i I_0(a_i)}. \quad (24)$$

From the laser light output expression we obtain the optical power out of the laser at the fundamental frequency and at the third-order intermodulation optical

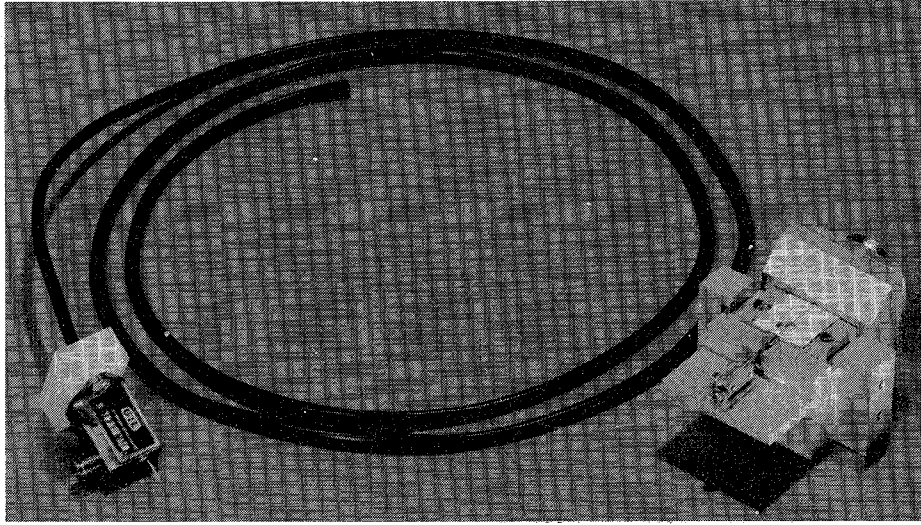


Fig. 5. Direct modulation fiber-optic link optimized for operation at 12 GHz.

power as

$$P_{\omega_1} = \frac{2P_0 I_1(a_1)}{I_0(a_1)} \cos(\omega_1 t), \quad (25)$$

$$P_{2\omega_2 - \omega_1} = \frac{2P_0 I_2(a_2) I_1(a_1)}{I_0(a_2) I_0(a_1)} \cos[(2\omega_2 - \omega_1)t]. \quad (26)$$

Thus we obtain IMD/C for small signals as

$$\frac{\text{IMD}}{C} = \frac{P_{2\omega_2 - \omega_1}}{P_{\omega_1}} = \frac{I_2(a_2)}{I_0(a_2)} \approx \frac{a_2^2}{8}. \quad (27)$$

At the third order intercept point the IMD/C ratio is equal to 1; hence using the value of  $a_2$  at the intercept we can define the value of modulation index  $m$  at the third order intercept as  $m_{\text{int}}$ . Therefore, the RF input power to the link and output power at the intercept point is calculated as

$$P_{\text{in, int}} = \frac{m_{\text{int}}^2 (I_b - I_{\text{th}})^2 |1 - S_{22L} \Gamma_{\text{Las}}|^2 Z_0}{|S_{21L}|^2 |1 - \Gamma_{\text{Las}}|^2}, \quad (28)$$

and

$$P_{\text{out, int}} = P_{\text{in, int}} \times G. \quad (29)$$

The 1 dB compression point is calculated in a similar fashion. For small input RF powers the output power at the fundamental frequency increases linearly with the input power, since

$$\frac{I_1(a_1)}{I_0(a_1)} = \frac{a_1}{2} \left[ \frac{1 + \frac{a_1^2}{8} + \frac{a_1^4}{192}}{1 + \frac{a_1^2}{4} + \frac{a_1^4}{64}} \right] \approx \frac{a_1}{2} \quad \text{for small } a_1. \quad (30)$$

Thus for small input RF powers the power at the fundamental frequency is

$$P_{\omega_1 \text{ linear}} = a_1 P_0 \cos(\omega_1 t + \theta_1). \quad (31)$$

At larger input RF powers the fundamental begins to saturate. This response can be obtained by considering more terms of the modified Bessel functions in the expression for the fundamental, which gives

$$P_{\omega_1 \text{ saturated}} = \frac{a_1}{3} \left[ \frac{a_1^4 + 24a_1^2 + 192}{a_1^4 + 16a_1^2 + 64} \right] P_0 \cos(\omega_1 t + \theta_1). \quad (32)$$

The RF power at the output of the link is given by

$$P_{\text{out rf}} = K_L^2 L^2 K_D^2 \eta_D^2 P_{\omega_1}^2 G_{RX} Z_0. \quad (33)$$

The 1 dB compression point is then calculated at the RF input power where the output power diverges from the linear gain by 1 dB, or in a linear form,

$$\frac{P_{\text{out, rf linear}}}{P_{\text{out, rf saturated}}} = \frac{P_{\omega_1 \text{ linear}}^2}{P_{\omega_1 \text{ saturated}}^2} = 1.2589, \quad (34)$$

giving  $a_1 = 1.00952$  at the 1 dB compression point. From this value of  $a_1$  we obtain the value of  $m$  [16]. On substituting the value of  $m$  at the 1 dB compression point in the expression for input RF power we obtain the input power at the 1 dB compression point as

$$P_{\text{in, 1 dB CP}} = \frac{m_{1 \text{ dB CP}}^2 (I_b - I_{\text{th}})^2 |1 - S_{22L} \Gamma_{\text{Las}}|^2 Z_0}{|S_{21L}|^2 |1 - \Gamma_{\text{Las}}|^2}, \quad (35)$$

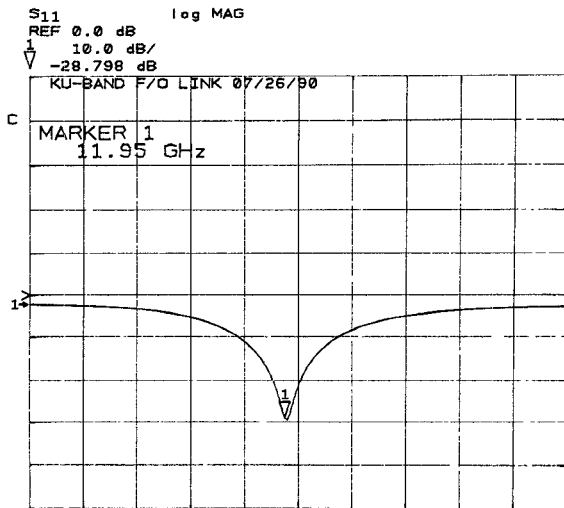
and

$$P_{\text{out, 1 dB CP}} = \frac{P_{\text{in, 1 dB CP}} \times G}{1.2589}. \quad (36)$$

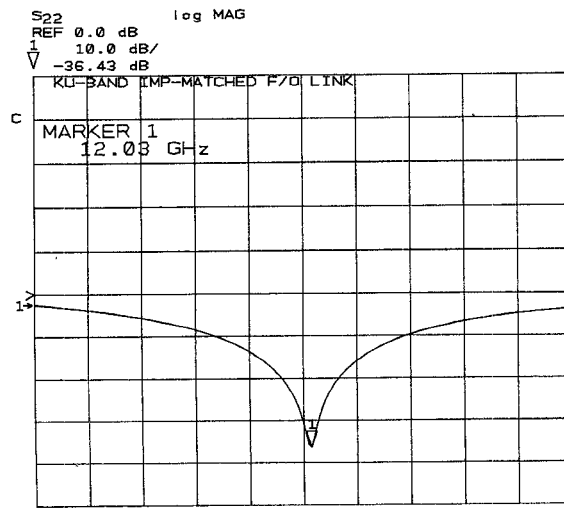
The spurious-free and compression dynamic ranges of the directly modulated FO link are defined as follows:

$$\text{SFDR} = \left( \frac{P_{\text{out, int}}}{N_{\text{out}}} \right)^{2/3}, \quad (37)$$

$$\text{CDR} = \frac{1.2589 \times P_{\text{out, 1 dB CP}}}{N_{\text{out}}}. \quad (38)$$



(a)



(b)

Fig. 6. Measured input and output return losses of the *Ku*-band (11.6–12.4 GHz) direct modulation fiber optic link, accomplished using single-stage reactive matching networks. (a) Return loss of the impedance-matched laser. (b) Return loss of the impedance-matched detector.

### Experiments

A direct modulation link was developed for operation at 11.6–12.4 GHz using an InGaAsP distributed-feedback laser diode. This device emits at the 1.3  $\mu\text{m}$  wavelength and features a responsivity of  $\eta_L = 0.26 \text{ mW/mA}$  when biased well above its threshold current of 13 mA. The detector used in the link was a single-mode fiber-pigtailed 1.3  $\mu\text{m}$ -wavelength p-i-n photodiode with a responsivity of  $\eta_D = 0.56 \text{ mA/mW}$  and a 3-dB modulation bandwidth of 15 GHz. The laser diode and photodetector had been mounted in standard microwave test fixtures to enable de-embedding of the device impedances out of the test fixtures. Based on the de-embedded equivalent circuit

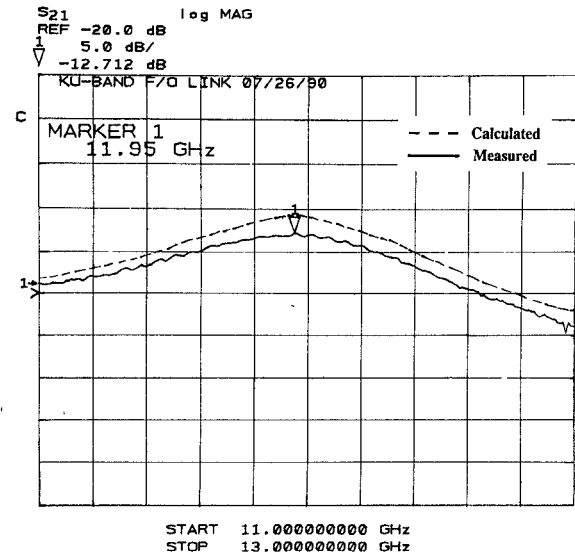


Fig. 7. Insertion loss comparison of the experimental and analytical results of a direct modulation fiber-optic link over the 11–13 GHz frequency range.

model of these devices, the Bode–Fano's theorem [17] predicts for a minimum return loss of 10-dB, reactive matching bandwidths greater than 6 GHz for the laser diode and 4 GHz for the photodetector at center frequency of 12 GHz can be obtained.

Using these devices optical transmitter and receiver modules were fabricated. The reactively matched optical interface modules are shown in Fig. 5, where a single-stage distributed matching network and the single-mode optical fiber coupling are visible in the optical transmitter. Narrowband reactive matching of the optical receiver was accomplished via internal modifications to a commercial photodetector package. The electrical input and outputs are 50  $\Omega$  microstrip transitions to SMA connectors. Measured 12 GHz return losses of 29 dB and 36 dB were obtained respectively for the laser and photodetector modules, as shown in Fig. 6, when inductances and capacitances that constitute the matching circuits were properly tweaked.

Optical power was coupled from the laser to the active region of the detector with an efficiency ( $K_L \cdot L \cdot K_D$ ) of 40% using a plano-convex gradient-index (GRIN) lens with AR-coated facets to focus the diverging output beam of the semiconductor laser into the 8  $\mu\text{m}$  core of the single-mode fiber. This resulted in a link current transfer function  $H_L = 0.058$  at 12 GHz. Based on this efficiency and on the equivalent circuit models of the laser and detector modules, the gain of the link was predicted using (8). This predicted gain is plotted as a function of frequency alongside the measured gain in Fig. 7. Both curves have 3-dB bandwidths of  $\sim 800 \text{ MHz}$  and peak at 12 GHz, where the analytically predicted response is  $-10.9 \text{ dB}$  compared to the measured gain of  $-12.6 \text{ dB}$ . The 1.7 dB difference may be accounted for by the discrepancy between the scattering parameters of the simulated

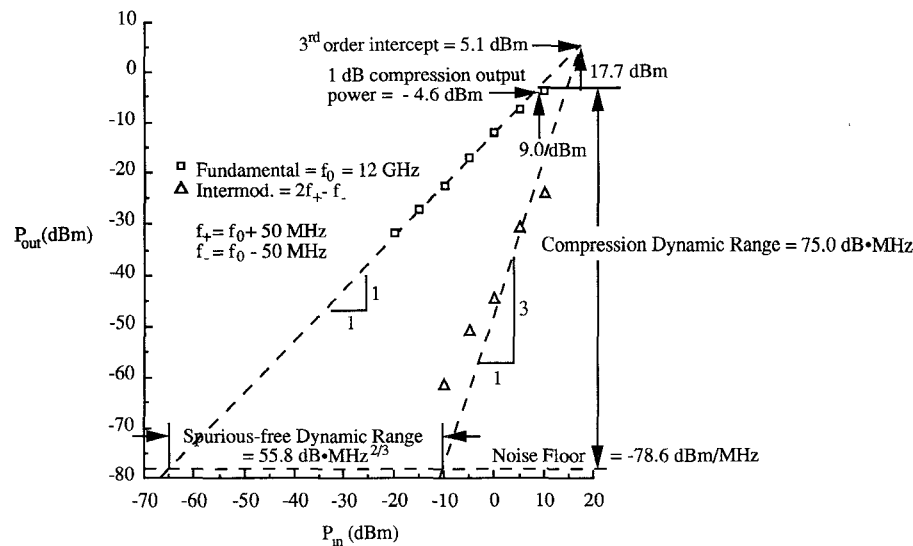


Fig. 8. Measured dynamic range of the experimental direct modulation fiber-optic link at 12 GHz.

matching network and those of the tweaked matching circuits.

Fig. 8 shows the plot of the measured direct modulation link output power versus input RF power of the fundamental and the third order intermodulation product at 12 GHz. It also shows the compression dynamic range and the spurious free dynamic range for the link obtained from measurements. The compression dynamic range is 75.0 dB in a 1 MHz receiver bandwidth, or 135.0 dB·Hz; the spurious free dynamic range is 55.8 dB·MHz<sup>2/3</sup> (95.8 dB·Hz<sup>2/3</sup>). The measured noise floor spectral power density level is -138.6 dBm/Hz. These results compare very favorably with the predicted spurious-free dynamic range of 97.3 dB·Hz<sup>2/3</sup> and noise floor spectral density of -140.1 dBm/Hz. Discrepancies between the predicted and measured performance parameters is partly due to lack of good data on the tweaked matching circuit and may also be caused in part by a number of phenomena that are difficult to quantify—for instance, the effect of finite optical reflections, such as from the input fiber end face back to the laser, upon laser noise and linearity.

### Discussion

The analysis and experimental results show how the gain, noise figure, and dynamic range of the direct modulation fiber-optic link could be improved. Obviously, higher electro-optic conversion efficiencies from the laser and detector would increase the gain, as would improvements in optical coupling efficiencies. Additionally, gain is proportional both to the transducer gain of the laser matching circuit, which is inversely proportional to the laser forward junction resistance, and to that of the photodetector matching circuit, which is inversely related to the reverse junction resistance and capacitance of the pin photodiode. As the desired operating bandwidth of the fiberoptic link is increased, the Q factors of the devices must be lowered according to Bode-Fano's theorem [17],

and thus the transducer gains of the laser and detector circuits will degrade, lowering gain that can be achieved.

Linear operation of a direct modulation fiber-optic link also depends largely on the ability to bias the laser diode at low modulation indices and away from the large-signal relaxation oscillation peak, which is dependent on the laser diode structure. To improve the dynamic range of the direct modulation link, laser diodes with lower RIN noise must be developed. For instance, semiconductor laser diode architectures involving the deposition of a reflective coating on the laser's rear facet (asymmetric) have demonstrated lower RIN noise than those with facets of equal reflectivity (symmetric) [16]. If efforts along these lines produce semiconductor lasers with noise approaching the shot-noise imposed low-noise limit, 10 dB lower noise figure and 6–8 dB·Hz<sup>2/3</sup> broader spurious-free dynamic range may be exhibited by direct modulation fiberoptic links. Approaches to increase the relaxation oscillation frequency of semiconductor lasers, thereby allowing modulation at higher frequencies and reducing the noise at a given frequency below the relaxation oscillation, often involve using distributed feedback structures rather than the Fabry-Perot architecture. Lower noise is ensured, however, only if the laser is shielded from optical feedback using an optical isolator between the laser and reflecting surfaces like the input end face of the optical fiber.

### EXTERNALLY MODULATED FO LINKS

#### Gain Analysis

The small-signal gain of an externally modulated fiber-optic link is derived using the SFD technique as was applied to direct modulation. When a lumped-element Mach-Zehnder interferometric modulator is employed in the optical transmitter to impress a microwave signal upon the optical carrier, the transmitter SFD is obtained by considering the capacitance  $C_m$  across the modulator



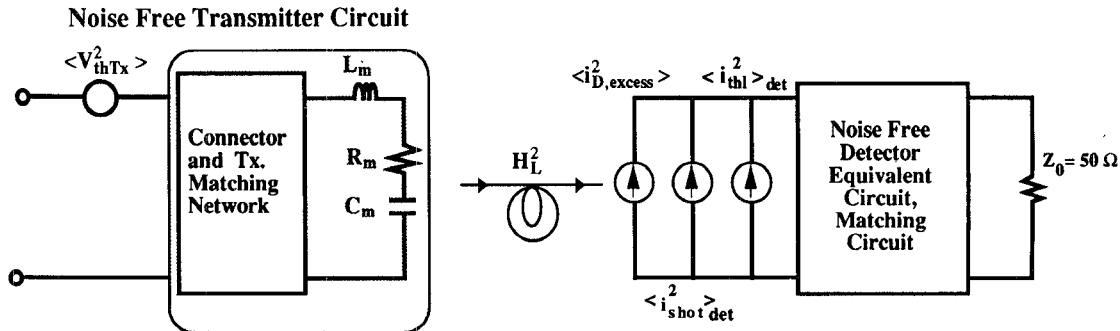


Fig. 9. Schematic representation of noise sources in an externally modulated FO link.

terminals to be the termination load  $\Gamma_M$  of a two-port network (represented by  $[S_M]$ ) consisting of the microwave impedance-matching circuit and the other device parameters in the equivalent circuit of the modulator, Fig. 2(a). Fig. 2(b) shows the SFD for the transmitter in an externally modulated FO link. The output power of a fiber-optic link depends on the amplitude of the detected photocurrent,  $I_{det}$ , which is in turn proportional to the RF voltage  $v_m$  across the capacitor  $C_m$ . This RF voltage is expressed as

$$v_m = \sqrt{Z_0} (a_{Lm} + b_{Lm}), \quad (39)$$

where  $a_{Lm}$  and  $b_{Lm}$  are the square roots of the incident and reflected powers at the modulator terminal capacitance and  $Z_0$  is the characteristic impedance of the input system (50  $\Omega$ ). From the SFD it is clear that

$$b_{Lm} = a_{Lm} \Gamma_M, \text{ and } a_{Lm} = \frac{b_{sm} S_{21m}}{1 - S_{22m} \Gamma_M} \text{ since } \Gamma_S = \Gamma_{SM} = 0, \quad (40)$$

where  $b_{sm}$  is the normalized incident transmitter power. Therefore,

$$|v_m| = \sqrt{\frac{Z_0 |b_{sm}|^2 |S_{21m}|^2 |1 + \Gamma_M|^2}{|1 - S_{22m} \Gamma_M|^2}} = \sqrt{\frac{Z_0 P_{in,Tx} |S_{21m}|^2 |1 + \Gamma_M|^2}{|1 - S_{22m} \Gamma_M|^2}}, \quad (41)$$

where  $P_{in,Tx}$  is the (unnormalized) RF input power to the external modulation link. Based on the  $P_{opt} - V$  curve of the lumped-element interferometric modulator, the optical output of the modulator can be represented in terms of the dc optical input  $P_{in,op}$  as

$$P_{out,op} = P_{in,op} \cos^2 \left( \frac{\pi}{4} - \frac{\pi V_M}{2V_\pi} \right) = \frac{P_{in,op}}{2} \left( 1 + \sin \left( \frac{\pi V_M}{V_\pi} \right) \right), \quad (42)$$

where  $V_M = V_b + v_m \sin \omega t$ ,  $V_\pi$  is the bias voltage required for 100% modulation, and  $V_b$  is the dc bias applied to the

modulator. For small signals the output reduces to

$$P_{out,op} = P_{in,op} \left( \frac{\pi v_m}{2V_\pi} \right) \cos \left( \frac{\pi V_b}{V_\pi} \right). \quad (43)$$

The detected photocurrent is defined

$$I_{det} = LK_D \eta_D P_{out,op}, \quad (44)$$

where  $L$ ,  $K_D$ , and  $\eta_D$  are as defined previously. Therefore, it is clear that

$$|I_{det}|^2 = \left( LK_D \eta_D \frac{\pi P_{in,op}}{2V_\pi} \right)^2 \cos^2 \left( \frac{\pi V_b}{V_\pi} \right) \frac{|S_{21M}|^2 |1 + \Gamma_M|^2}{|1 - \Gamma_M S_{22M}|^2} \cdot Z_0 P_{in,Tx}. \quad (45)$$

Using the expression for  $G_{Rx}$  previously derived, the small-signal gain of the external modulation link operated at its linear dc bias voltage is obtained:

$$G = \left( LK_D \eta_D \frac{\pi P_{in,op} Z_0}{2V_\pi} \right)^2 \cos^2 \left( \frac{\pi V_b}{V_\pi} \right) \frac{|S_{21M}|^2 |S_{21D}|^2 |1 + \Gamma_M|^2}{|1 - \Gamma_M S_{22M}|^2 |1 - \Gamma_{SD} S_{11D}|^2}. \quad (46)$$

### Noise Analysis

The noise analysis of the externally modulated link is performed in manner almost identical to that of the directly modulated link. Fig. 9 shows the schematic of the externally modulated link with the noise sources categorized as the transmitter's thermal and excess noise and the receiver's thermal and shot noise.

The transmitter's thermal noise sources are represented as one equivalent thermal noise voltage at the transmitter's input. This noise voltage is then transformed into the noise power at the output of the link, using the gain across the complete link, as

$$N_{thtx} = 2kT_a B \left( \frac{\pi LK_D \eta_D P_{in,op} Z_0}{2V_\pi} \right)^2 \cos^2 \left( \frac{\pi V_b}{V_\pi} \right) \frac{|S_{21M}|^2 |S_{21D}|^2 |1 + \Gamma_M|^2}{|1 - \Gamma_M S_{22M}|^2 |1 - \Gamma_{SD} S_{11D}|^2}. \quad (47)$$

The excess noise of the laser warrants some explanation. The  $\langle i_{D,excess}^2 \rangle$  term is the excess noise arising from

relaxation oscillations in the optical source, and is deduced from spectral power density measurements of the unmodulated output power of the laser. However it can also be calculated from the manufacturer's quoted RIN which includes the shot noise contribution of the receiver as well. This calculation is given as

$$\text{RIN} = \frac{2eI_{\text{dc}} + \langle i_{D,\text{excess}}^2 \rangle}{I_{\text{dc}}^2}, \quad (48)$$

where  $I_{\text{dc}}$ , the dc-detected photocurrent for the given output power from the modulator, is simply

$$I_{\text{dc}} = \frac{LK_D \eta_D P_{\text{in,op}}}{2} \left( 1 + \sin \frac{\pi V_b}{V_\pi} \right). \quad (49)$$

From this expression we can find the expression for the excess noise power as

$$N_{\text{excess}} = \left[ \frac{LK_D \eta_D P_{\text{in,op}}}{2} \left( 1 + \sin \frac{\pi V_b}{V_\pi} \right) \text{RIN}(I_b, f) - 2e \right] \times \frac{LK_D \eta_D P_{\text{in,op}}}{2} \left( 1 + \sin \frac{\pi V_b}{V_\pi} \right) B \frac{|S_{21D}|^2}{|1 - \Gamma_{sD} S_{11D}|^2} Z_0. \quad (50)$$

The receiver thermal noise power is given as (12). The shot noise of the detector, including the dark current,  $I_d$ , is denoted by a current source at the input of the receiver. This current source is transferred to output by  $G_{RX}$  and the output impedance to represent the shot noise power as

$$N_{\text{shot}} = 2e \left[ \frac{LK_D \eta_D P_{\text{in,op}}}{2} \left( 1 + \sin \frac{\pi V_b}{V_\pi} \right) + I_d \right] \cdot B \frac{|S_{21D}|^2}{|1 - \Gamma_{sD} S_{11D}|^2} Z_0. \quad (51)$$

The total noise power at the output of the optical detector module is the sum of all these individual noise powers. For actively matched optical detectors, the noise contribution from the amplifier should be incorporated as was presented in the direct modulated case, but this will be omitted here. The noise power at the input to the external modulation link is simply  $kT_a B$ . Equation (21) gives the noise figure, with the  $N_{\text{out}}$  term defined as the sum of (12), (47), (50), and (51).

#### Distortion Analysis

The distortion characteristics of the external modulation link are analyzed with respect to the modulation index  $m$ , which for a Mach-Zehnder modulator at a dc bias point  $V_b$  is defined as

$$m = \frac{v_m}{\frac{V_\pi}{2} - |V_b|} = \frac{2v_m}{V_\pi - 2|V_b|}. \quad (52)$$

By letting  $V_M = V_b + v_m(\sin \omega_1 t + \sin \omega_2 t)$  and substituting into (42), an expression is obtained for the optical power at fundamental frequency:

$$P_{\omega_1} = P_{\text{in,op}} J_0(a) J_1(a) \cos \frac{\pi V_b}{V_\pi} \sin \omega_1 t, \quad (53)$$

and at the frequency of one of the third-order intermodulation products:

$$P_{2\omega_2 - \omega_1} = P_{\text{in,op}} J_1(a) J_2(a) \cos \frac{\pi V_b}{V_\pi} \sin(2\omega_2 - \omega_1)t, \quad (54)$$

where we have defined  $a = \pi v_m / V_\pi$ . Therefore, the ratio of third-order intermodulation product output power to that of the fundamental is dependent only on the small-signal modulation voltage  $v_m$  and not upon the dc bias level  $V_b$ . Specifically,

$$\frac{\text{IMD}}{C} = \frac{P_{2\omega_2 - \omega_1}}{P_{\omega_1}} = \frac{J_2(a)}{J_0(a)} \quad (55)$$

Given the Taylor series expansions of the 0th and 2nd order Bessel functions:

$$J_0(a) = 1 - \frac{a^2}{4} + \frac{a^4}{64} - \dots \quad (56)$$

$$J_2(a) = \frac{a^2}{8} \left( 1 - \frac{a^2}{12} + \frac{a^4}{384} - \dots \right), \quad (57)$$

we find that for small signals

$$\frac{\text{IMD}}{C} \cong \frac{a^2}{8} = \frac{1}{8} \left( \frac{\pi v_m}{V_\pi} \right)^2 = \frac{\pi^2 m^2}{32} \left( 1 - \frac{2|V_b|}{V_\pi} \right)^2. \quad (58)$$

The small-signal behavior of the fundamental and third-order intermodulation product is extrapolated to determine the modulation index at the third-order intercept—i.e., where  $\text{IMD}/C = 1$ :

$$m_{\text{int}} = \frac{\sqrt{32}}{\pi \left( 1 - \frac{2|V_b|}{V_\pi} \right)}. \quad (59)$$

By expressing the RF input power to the link in terms of the modulation index  $m$  rather than modulation voltage  $v_m$  and substituting  $m = m_{\text{int}}$ , we obtain the input power at the third order intercept as

$$P_{\text{in,int}} = \frac{m_{\text{int}}^2 (V_\pi - 2|V_b|)^2 |1 - S_{22m} \Gamma_M|^2}{4 Z_0 |S_{21m}|^2 |1 + \Gamma_M|^2}. \quad (60)$$

and

$$P_{\text{out,int}} = P_{\text{in,int}} \times G, \quad (61)$$

where  $G$  is the gain. For small input RF powers the output power at the fundamental frequency increases

linearly with the input power, since

$$J_1(a)J_0(a) = \frac{a}{2} \left( 1 - \frac{a^2}{8} + \frac{a^4}{192} - \dots \right) \left( 1 - \frac{a^2}{4} + \frac{a^4}{64} - \dots \right) \approx \frac{a}{2} \text{ for small } a. \quad (62)$$

At larger input RF powers the fundamental begins to saturate. This response is obtained by considering more terms of the Bessel function. Compression of the fundamental output power by 1 dB means that

$$\frac{P_{\text{out,rf linear}}}{P_{\text{out,rf saturated}}} = \frac{P_{\omega_1 \text{ linear}}^2}{P_{\omega_1 \text{ saturated}}^2} = 1.2589, \quad (63)$$

where  $P_{\omega_1}$  is given by (53). Therefore, 1 dB of AM compression occurs when

$$\frac{\frac{a^2}{4}}{\left( 1 - \frac{a^2}{4} + \frac{a^4}{64} - \dots \right)^2 \frac{a^2}{4} \left( 1 - \frac{a^2}{8} + \frac{a^4}{192} - \dots \right)^2} = 1.2589, \quad (64)$$

which corresponds to  $a = 0.5500$ . From this value of  $a = (\pi V_m / V_\pi)$ , (52) is used to obtain the value of the modulation index  $m$  at the point of 1 dB compression. Substituting this into the equation for input RF power in terms of modulation index  $m$ , the input power at the 1 dB compression point is

$$P_{\text{in, 1 dB CP}} = \frac{(0.5500)^2 V_\pi^2 |1 - S_{22m} \Gamma_M|^2}{\pi^2 Z_0 |S_{21m}|^2 |1 + \Gamma_M|^2}, \quad (65)$$

$$P_{\text{out, 1 dB CP}} = \frac{P_{\text{in, 1 dB CP}} \times G}{1.2589}. \quad (66)$$

The spurious-free and compression dynamic ranges of the external modulation link are defined exactly as they are for the direct modulation link, i.e.:

$$\text{SFDR} = \left( \frac{P_{\text{out,int}}}{N_{\text{out}}} \right)^{2/3}, \quad (67)$$

$$\text{CDR} = \frac{1.2589 \times P_{\text{out, 1 dB CP}}}{N_{\text{out}}}. \quad (68)$$

### Experiments

An externally modulated FO link was developed at 875–925 MHz to examine the validity of the analytical model. A  $1.3 \mu\text{m}$  LiNbO<sub>3</sub> Mach–Zehnder interferometric modulator with a lumped-element electrode structure was selected. The device exhibited a 23 dB extinction ratio when TE-polarized light was launched into its polarization-preserving input single-mode fiber pigtail. In addition, a switching voltage  $V_\pi = 8.3$  V and a 3-dB modulation bandwidth of 3 GHz were quoted by the manufacturer. An InGaAs p-i-n photodiode with a responsivity

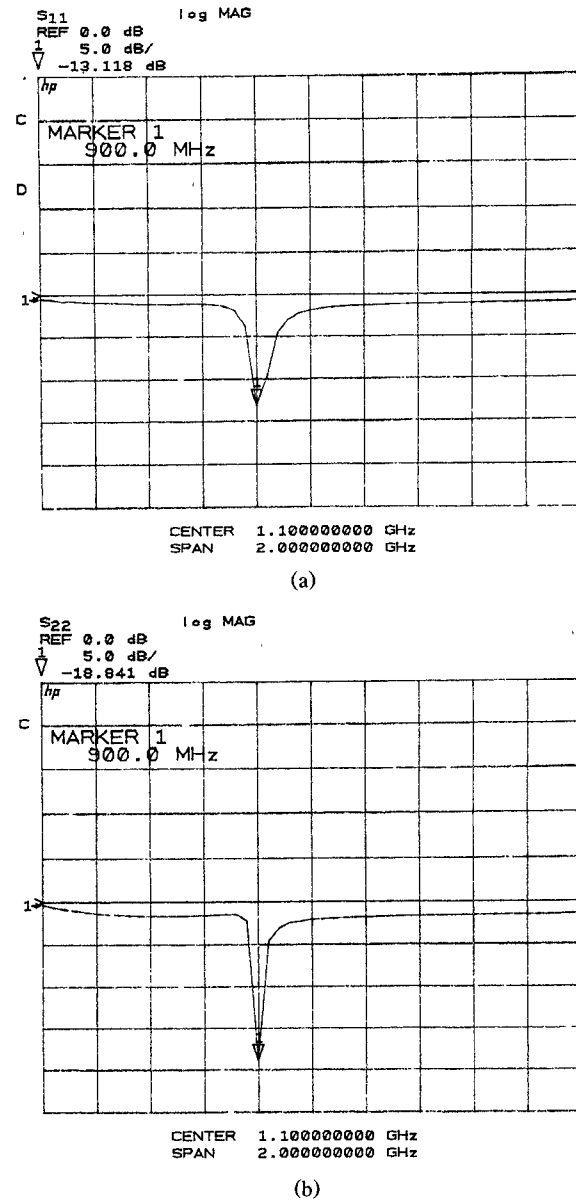


Fig. 10. Measured input and output return losses of the L-band (875–925 MHz) external modulation fiber-optic link, accomplished using single-stage reactive matching networks. (a) Return loss of the impedance-matched modulator. (b) Return loss of the impedance-matched detector.

$\eta_D = 1.0$  mA/mW and frequency response bandwidth of 10 GHz was employed in the optical receiver.

Using the scattering parameters of the modulator and photodetector, de-embedded from the measured S-parameters, equivalent circuit models were developed by fitting them to the measured impedance. This made possible the design and construction of single-stage reactive circuits to impedance-match the electro-optic devices to  $50 \Omega$  at the link design frequency of 900 MHz. Based on the external Q-factors of these devices, Bode–Fano’s theorem predicts that for 10-dB minimum return loss at the center frequency of 900 MHz, reactive matching bandwidths of only 115 MHz for the lumped-element

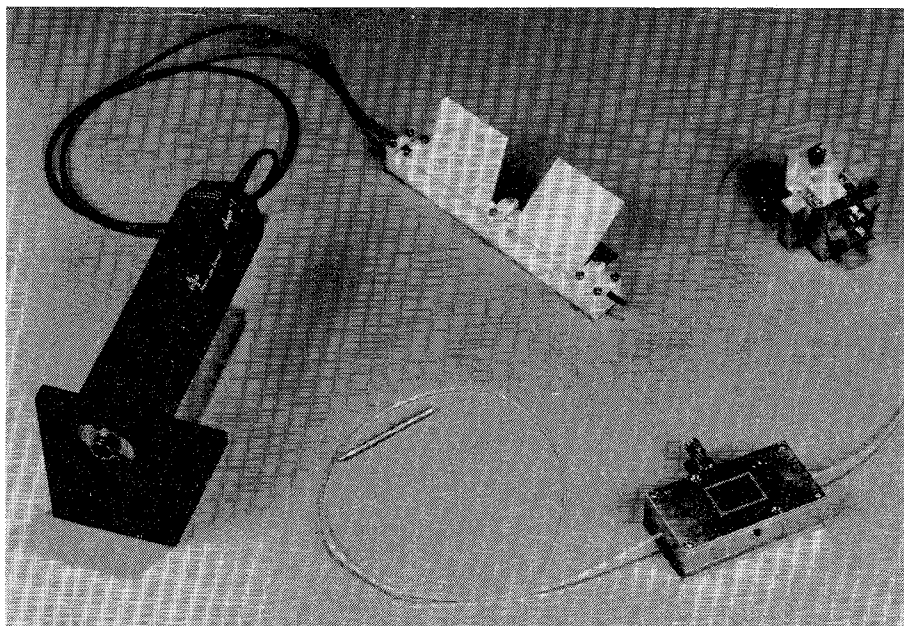


Fig. 11. Experimental *L*-band external modulation fiber-optic link consisting of (left to right) a high-power (60 mW) single-mode fiber-pigtailed solid-state laser, optical polarization controller, and impedance-matched modulator and detector modules.

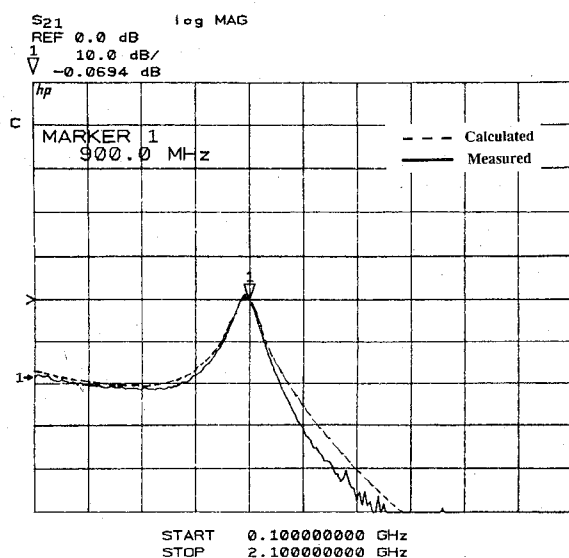


Fig. 12. Insertion loss comparison of the experimental and analytical results of an external modulation fiber-optic link over the 0.1–2.1 GHz frequency range.

modulator and 60 MHz for the reverse-biased photodetector can be obtained. Measured input and output 900 MHz return losses of 13 dB and 18 dB were obtained (Fig. 10) when matching circuits were constructed and properly tweaked. In the figure, actual  $-10$  dB return loss bandwidths of 50 MHz for the input and 40 MHz for the output are apparent.

In order to maximize the gain and dynamic range of the external modulation link, large optical pump power—60 mW at  $\lambda = 1.3 \mu\text{m}$ —was obtained from a single-mode fiber-pigtailed Nd:YAG laser source. The solid-state laser and the optical receiver were optically coupled to the

modulator's input and output fibers, respectively, and the input optical polarization was adjusted to maximize the ratio of optical power measured at the "ON" and "OFF" state switch voltages. The photograph of the externally modulated FO link consisting of the solid-state laser, polarization control device, and reactively matched 900 MHz modulator and photodetector modules, is shown in Fig. 11.

At the modulator's linear, half-power bias point, a dc photodetected current  $I_{dc} = (LK_D \eta_D P_{in,op})/2 = 4.3$  mA was measured. Based on this measurement and on the scattering parameters derived from the equivalent circuit model of the externally modulated FO link, (46) was used to predict the small-signal gain for the frequency range of 0.1–2.1 GHz. This calculated result is plotted as a function of frequency in Fig. 12 along with the measured gain. Especially at the design frequency of 900 MHz where both peak at the gain of 0 dB, the agreement between the predicted and measured gain curves is excellent. Both curves show a 3-dB link bandwidth of approximately 50 MHz.

A two-tone intermodulation distortion measurement was performed to determine the spurious-free and compression dynamic ranges of the external modulation fiber-optic link at its center frequency of 900 MHz. Fig. 13 shows the results of the intermodulation distortion measurement as well as the measured output noise floor of the link. The thermal noise of the modulator and detector and the dark current and short noise power were calculated using (12), (47), and (51), and the excess noise was determined by subtracting the sum of these noise powers from the measured total noise floor  $P_{N,out}$ . A noise figure of 24.3 dB was measured at 900 MHz. As shown, the measured 1 dB compression and third-order

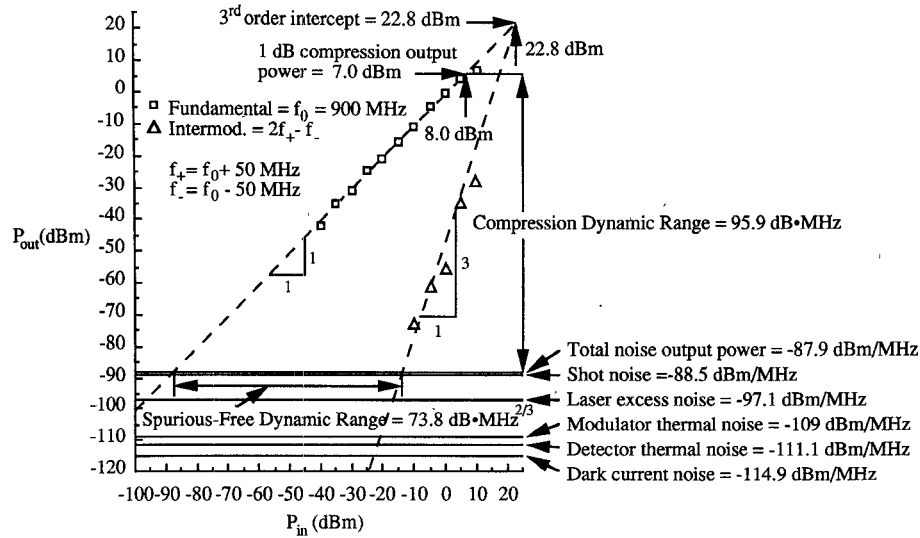


Fig. 13. Results of a two-tone intermodulation distortion measurement, showing the 1 dB compression and third order intercept points of the external modulation link at 900 MHz. Also plotted are the calculated noise powers contributing to the measured output noise floor in a 1 MHz bandwidth. The link's 95.9 dB·MHz compression dynamic range and spurious-free dynamic range of 73.8 dB·MHz<sup>2/3</sup> are rendered as well.

intercept output powers are 7 dBm and 22.8 dBm, respectively. Thus, the compression dynamic range under these conditions is 95.9 dB·MHz (155.9 dB·Hz) and the spurious-free dynamic range is 73.8 dB·MHz<sup>2/3</sup> (113.8 dB·Hz<sup>2/3</sup>), the largest dynamic range reported to date for any microwave fiber-optic link. These results very closely match the predicted noise figure and spurious-free dynamic range values of 24.1 dB and 112.7 dB·Hz<sup>2/3</sup>. It was observed that the measured  $P$ - $V$  curve of the modulator deviated from perfect sinusoidal behavior, which may have created some discrepancy between predicted and measured performance parameters since Bessel functions cannot accurately predict the 1 dB compression and third-order intercept points in such an instance.

### Discussion

This analytical model clearly indicates that the available optical source power must be maximized to improve the external modulation link performance. Not only is the link gain proportional to  $P_{in,op}^2$ , but since the shot noise dominates over the RIN of the solid-state laser the noise floor increases proportional only to  $P_{in,op}$ . Therefore, if very high optical power can be attained without saturating the modulator, the external modulation link will approach its noise figure limit of 3 dB. This amounts to a 21 dB improvement in noise figure, and consequently a 14 dB·Hz<sup>2/3</sup> improvement in spurious-free dynamic range over the results presented here.

The ability of the detector to handle a large reverse bias and high incident optical powers is necessary before the external modulation link noise figure can approach its thermal noise limit of 3 dB, which would maximize the link's dynamic range. Detector design may be even more critical in the external modulation link than in the direct

modulation link since modulation of very high optical power remains linear up to high RF powers which may saturate the photodetector.

### CONCLUSION

Complete analytical models of direct and external modulation fiberoptic link performance have been presented and experimentally verified. Consequently, the potential for very high gain and wide dynamic range has been demonstrated by the analytical approach, especially in the case of the external modulation link with the Nd:YAG laser as its optical source. An experimental  $Ku$ -band (11.6–12.4 GHz) fiber-optic link was designed and constructed using the direct modulation link models, and featured a minimum insertion loss of -12.6 dB at 12 GHz and a spurious-free dynamic range of 95.8 dB·Hz<sup>2/3</sup>. An experimental  $L$ -band (875–925 MHz) fiber-optic link designed using the external modulation models exhibited a peak RF insertion gain of 0 dB and compression and spurious-free dynamic ranges of 155.9 dB·Hz and 113.8 dB·Hz<sup>2/3</sup>, respectively.

The analytical models not only allow for a pre-design comparison of link architectures to achieve a given level of performance, but also specify what must be done in order to improve any given performance parameter. The equations predicting the various performance parameters are functions of the laser dc bias current in the case of direct modulation and modulator dc bias voltage in the case of external modulation. In this paper results were reported and discussed at the bias settings at which the RF insertion gain of each link was maximum. The dependence of the performance parameters upon the bias conditions is more complex in both the direct and external modulation scenarios, and this expansive subject is reported elsewhere [15], [16], and [18].

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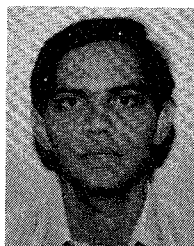
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